

$a^n b^n c^n$ Language

grammar AnBnCn

nonterminal B(2), A(4), S(0);
terminal a(2), b(2), c(2);
start S;

S() ::= B(x,y) [init]
B(u,v) ::= a(u,x) b(x,v) c(v,w) [init1]
| a(u,x) b(y,v) c(v,z) A(x,y,z,w) [init2]
A(n1,n2,n3,n4) ::= a(n1,x) b(y,n2) c(n3,z) A(x,y,z,n4) [a1]
| a(n1,x) b(x,n2) c(n3,n4) [a2]

end

State $q_0(a, b)$

S()	→ . B(a, b)
B(a, b)	→ . a(a, n ₁) b(n ₁ , b) c(b, n ₂)
B(a, b)	→ . a(a, n ₃) b(n ₄ , b) c(b, n ₅) A(n ₃ , n ₄ , n ₅ , n ₆)

$$\frac{B(n_0, n_1)}{n_0 = a, n_1 = b} \rightarrow q_{12}(n_0, n_1)$$

$$\frac{a(n_0, n_1)}{n_0 = a, n_1 \uparrow} \rightarrow q_1(n_0, b, n_1, b)$$

State $q_1(a, b, c, b)$

B(a, b)	→ a(a, c) . b(c, b) c(b, n ₁)
B(a, b)	→ a(a, c) . b(n ₂ , b) c(b, n ₃) A(c, n ₂ , n ₃ , n ₄)

$$\frac{b(n_0, n_1)}{n_0 = c, n_1 = b} \rightarrow q_3(a, n_1, n_0)$$

$$\frac{b(n_0, n_1)}{n_0 \uparrow, n_1 = b} \rightarrow q_2(a, n_1, c, n_0)$$

State $q_2(a, b, c, d)$

B(a, b)	→ a(a, c) b(d, b) . c(b, n ₁) A(c, d, n ₁ , n ₂)
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$$\frac{c(n_0, n_1)}{n_0 = b, n_1 \uparrow} \rightarrow q_4(a, n_0, c, d, n_1)$$

State $q_3(a, b, c)$

B(a, b)	→ a(a, c) b(c, b) . c(b, n ₁)
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$$\frac{c(n_0, n_1)}{n_0 = b, n_1 \uparrow} \rightarrow q_5(a, n_0, c, n_1)$$

State $q_4(a, b, c, d, e)$

B(a, b)	→ a(a, c) b(d, b) c(b, e) . A(c, d, e, n ₁)
A(c, d, e, n ₂)	→ . a(c, n ₃) b(n ₃ , d) c(e, n ₂)
A(c, d, e, n ₄)	→ . a(c, n ₅) b(n ₆ , d) c(e, n ₇) A(n ₅ , n ₆ , n ₇ , n ₄)

$$\frac{A(n_0, n_1, n_2, n_3)}{n_0 = c, n_1 = d, n_2 = e, n_3 \uparrow} \rightarrow q_{13}(a, b, n_0, n_1, n_2, n_3)$$

$$\frac{a(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_6(n_0, d, e, n_1, d, e)$$

State $q_5(a, b, c, d)$

B(a, b)	→ a(a, c) b(c, b) c(b, d) . [init1]
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State $q_6(a, b, c, d, b, c)$

A(a, b, c, n ₁)	→ a(a, d) . b(n ₂ , b) c(c, n ₃) A(d, n ₂ , n ₃ , n ₁)
A(a, b, c, n ₄)	→ a(a, d) . b(d, b) c(c, n ₄)

$$\frac{b(n_0, n_1)}{n_0 = d, n_1 = b} \rightarrow q_7(a, n_1, c, n_0)$$

$$\frac{b(n_0, n_1)}{n_0 \uparrow, n_1 = b} \rightarrow q_8(a, n_1, c, d, n_0)$$

State $q_7(a, b, c, d)$

$$\boxed{A(a, b, c, n_1) \rightarrow a(a, d) b(d, b) \cdot c(c, n_1)}$$

$$\frac{c(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_9(a, b, n_0, n_1, d)$$

State $q_8(a, b, c, d, e)$

$$\boxed{A(a, b, c, n_1) \rightarrow a(a, d) b(e, b) \cdot c(c, n_2) A(d, e, n_2, n_1)}$$

$$\frac{c(n_0, n_1)}{n_0 = c, n_1 \uparrow} \rightarrow q_{10}(a, b, n_0, d, e, n_1)$$

State $q_9(a, b, c, d, e)$

$$\boxed{A(a, b, c, d) \rightarrow a(a, e) b(e, b) c(c, d) \cdot [a^2]}$$

State $q_{10}(a, b, c, d, e, f)$

$$\boxed{A(a, b, c, n_1) \rightarrow a(a, d) b(e, b) c(c, f) \cdot A(d, e, f, n_1)}$$

$$\boxed{A(d, e, f, n_2) \rightarrow \cdot a(d, n_3) b(n_3, e) c(f, n_2)}$$

$$\boxed{A(d, e, f, n_4) \rightarrow \cdot a(d, n_5) b(n_6, e) c(f, n_7) A(n_5, n_6, n_7, n_4)}$$

$$\frac{A(n_0, n_1, n_2, n_3)}{n_0 = d, n_1 = e, n_2 = f, n_3 \uparrow} \rightarrow q_{11}(a, b, c, n_3, n_0, n_1, n_2)$$

$$\frac{a(n_0, n_1)}{n_0 = d, n_1 \uparrow} \rightarrow q_6(n_0, e, f, n_1, e, f)$$

State $q_{11}(a, b, c, d, e, f, g)$

$$\boxed{A(a, b, c, d) \rightarrow a(a, e) b(f, b) c(c, g) A(e, f, g, d) \cdot [a^1]}$$

State $q_{12}(a, b)$

$$\boxed{S() \rightarrow B(a, b) \cdot [init]}$$

State $q_{13}(a, b, c, d, e, f)$

$$\boxed{B(a, b) \rightarrow a(a, c) b(d, b) c(b, e) A(c, d, e, f) \cdot [init^2]}$$